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Thermostatic properties of nitrate molten salts and their solar and eutectic mixtures

B. D'Aguanno¹, M. Karthik², A. N. Grace¹ & A. Floris³ 

Nitrate molten salts are extensively used for sensible heat storage in Concentrated Solar Power (CSP) plants and thermal energy storage (TES) systems. They are the most promising materials for latent heat storage applications. By combining classical molecular dynamics and differential scanning calorimetry experiments, we present a systematic study of all thermostatic, high temperature properties of pure KNO_3 and NaNO_3 salts and their eutectic and "solar salt" mixtures, technologically relevant. We first study, in solid and liquid regimes, their mass densities, enthalpies, thermal expansion coefficients and isothermal compressibilities. We then analyze the c_p and c_v specific heats of the pure salts and of the liquid phase of the mixtures. Our theoretical results allow to resolve a long-standing experimental uncertainty about the $c_p(T)$ thermal behaviour of these systems. In particular, they revisit empirical laws on the $c_p(T)$ behaviour, extensively used at industrial level in the design of TES components employing the "solar salt" as main storage material. Our findings, numerically precise and internally consistent, can be used as a reference for the development of innovative nanomaterials based on nitrate molten salts, crucial in technologies as CSP, waste heat recovery, and advanced adiabatic compressed air energy storage.

Molten salts are the most used materials for thermal energy storage at high temperature. This is due to several physical properties that they exhibit, which are important in industrial applications related to energy. The first factor affecting the performance of a thermal energy storage (TES) system is the thermal stability of the materials used to store heat, i.e. the temperature interval where they are liquid. The thermal stability of nitrate molten salts (MNO_3 , M = alkali metal), allows the heat to be stored between ≈ 520 K and ≈ 890 K, an extended range of very high temperatures. This interval is typical for pure alkali nitrates (LiNO_3 , NaNO_3 , KNO_3), while their mixtures show a lower freezing point (e.g. for the eutectic NaNO_3 - KNO_3 mixture this is 495 K). This even larger thermal stability range fits the requirements of Concentrated Solar Power (CSP) plants which, as a consequence, use nitrate molten mixtures as a heat storage medium. By 2030, it is estimated a usage of $\approx 1.8 \times 10^9$ tons of nitrate mixtures in CSP plants¹.

Despite this extensive use of molten salts in thermal energy management, many basic and challenging issues about these materials are still unresolved, both at the experimental and theoretical level. One crucial issue is the temperature dependence of $c_p(T)$ in their liquid phase, especially concerning nitrate molten mixtures. Experimentally, different dependencies have been found, from increasing, to constant, to decreasing with T^{2-7} . For this reason, round robin tests have been launched within the scientific and technological communities⁸.

A technologically relevant nitrate mixture is the so called "solar salt", which has a weight fraction composition given by $x_{\text{NaNO}_3} = 0.6$ and $x_{\text{KNO}_3} = 1 - x_{\text{NaNO}_3} = 0.4$. Industrially, for this mixture the most used empirical equation for the mass density $\rho(T)$, at atmospheric pressure and within 530–890 K, is the function $\rho(T) = \alpha - \beta T$, where $\alpha = 2.09$ and $\beta = 0.000636^9$. The empirical relation used for the specific heat is the *T*-increasing function $c_p(T) = \gamma + \delta T$ where $\gamma = 1.443$ and $\delta = 0.000172^9$ (the units of T , $\rho(T)$ and $c_p(T)$ are K, g cm^{-3} and $\text{J g}^{-1} \text{K}^{-1}$, respectively). This last equation is the result of many experimental measurements and statistical analyses all based on the use of Differential Scanning Calorimetry (DSC)^{10,11}. However, an increasing $c_p(T)$ behaviour is more typical of weakly interacting liquids¹², while nitrates belong to the class of strongly interacting ones.

¹Centre for Nanotechnology Research, VIT University, Vellore, 632014, Tamil Nadu, India. ²Centre for Nanomaterials, International Advanced Research Centre for Powder Metallurgy and New Materials (ARCI), Balapur, Hyderabad, 500005, India. ³School of Mathematics and Physics, University of Lincoln, Brayford Pool, LN6 7TS, Lincoln, United Kingdom. Correspondence and requests for materials should be addressed to B.D. (email: bruno.daguanno@protonmail.com) or M.K. (email: mkarthik@project.arci.res.in) or A.F. (email: afloris@lincoln.ac.uk)

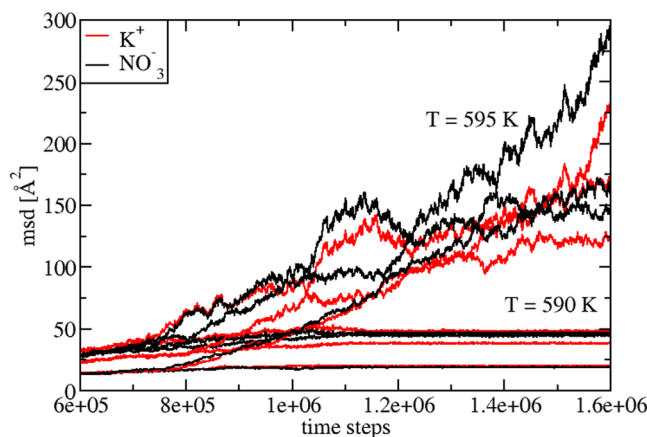


Figure 1. Mean squared displacement (msd) of K^+ and NO_3^- ions, as a function of the molecular dynamics (MD) time steps. Data are shown for two temperatures, $T = 590$ K and $T = 595$ K. They are, respectively, immediately below and above the calculated melting temperature $T_M^{MD} = 592.5$ K. Three cartesian components for each T are shown. At $T = 590$ K a typical solid-like constant behavior is evident, while at $T = 595$ K the plot exhibits a completely different, liquid-like behavior.

In this rather complex experimental scenario, systematic theoretical results about thermostatic properties of molten salts and their mixtures are largely missing, while results for enthalpy $H(T)$ and $c_p(T)$ of pure salts have been reported in ref.¹³.

As mentioned, empirical equations represent a key factor in establishing TES performances and have been crucial in the design of state-of-the-art CSP plants built recently¹⁴. Thus, revisiting them theoretically has a potentially high technological impact. Here, the validity of the mentioned c_p relation will be investigated in detail and critically reconsidered.

Clearly, improvements in the performances of storage systems, connected to the energy production and reduction of electricity costs (e.g., of CSP plants), heavily rely on the maximum optimization of the thermodynamic properties of well known and new salt-based mixtures^{15–19}.

In this work, we perform an extensive theoretical analysis, based on classical molecular dynamics (MD), of the temperature behavior of the thermostatic properties of $NaNO_3$, KNO_3 and their mixtures, with emphasis on the thermal behaviour of the specific heats $c_p(T)$ and $c_v(T)$, technologically relevant especially for the mixtures. The results are first compared with our new DSC experiments and with previous measurements. Then, they are interpreted by establishing a link between the solid-state approach to collective vibrational modes in liquids^{20–23}, and the more standard gas-like approach^{24,25}.

Our analysis is devoted to (i) provide a theoretical characterization, both in the solid and liquid phases, of the thermostatic properties of nitrate molten salts; (ii) resolve the issues related to the $c_p(T)$ thermal behavior in the liquid phase of relevant salt mixtures; (iii) validate the MD model¹³ accuracy, for further studies about, e.g., nanofluids where the suspending medium are the nitrate salts studied here. The first two points are relevant for all the applications in the CSP technology and more generally in the field of renewable energy; the third, to develop an accurate theoretical framework able to study the thermodynamic properties of salt-based fluids for thermal energy storage^{15–19}. Our calculations are supported by a self-consistency check on the precision of our numerical methodology, only possible thanks to the fact that *all* relevant thermostatic properties were investigated.

Results

We will first investigate the thermostatic properties of pure potassium and sodium nitrates, in their solid and liquid regimes. Next, we will analyze the eutectic and “solar” mixtures with the ultimate goal to characterize the thermal behaviour of the specific heats in the liquid phases. All properties and methods to calculate them are described in the Methods Sections (MS).

Potassium Nitrate KNO_3 . Melting temperature. In order to study via MD the KNO_3 properties in a large temperature regime including various phases, the starting point is to locate the solid-to-liquid transition temperature T_M , at $P = 1$ atm. We find $T_M^{MD} = 592.5 \pm 2.5$ K, which is very close to the experimental value, $T_M^{exp} = 607$ K. This excellent agreement gives a first indication of the accuracy of the inter-atomic potentials used¹³.

Moreover, it is also the result of a MD procedure to locate T_M , based on the temporal evolution of a two-phase system, as described in MS 1.4. The melting point is also reported in ref.¹³, where a different value ($T_M = 513$ K \pm 17 K) was obtained via a thermodynamic integration-based method.

By following our procedure, in Fig. 1 we show the evolution of the three Cartesian components of the mean squared displacement (msd) of K^+ and NO_3^- at $T = 590$ K and $T = 595$ K. At $T = 590$ K ($< T_M^{MD}$), the msd shows a typical solid-like constant behavior, while at $T = 595$ K ($> T_M^{MD}$), a typical liquid-like behavior.

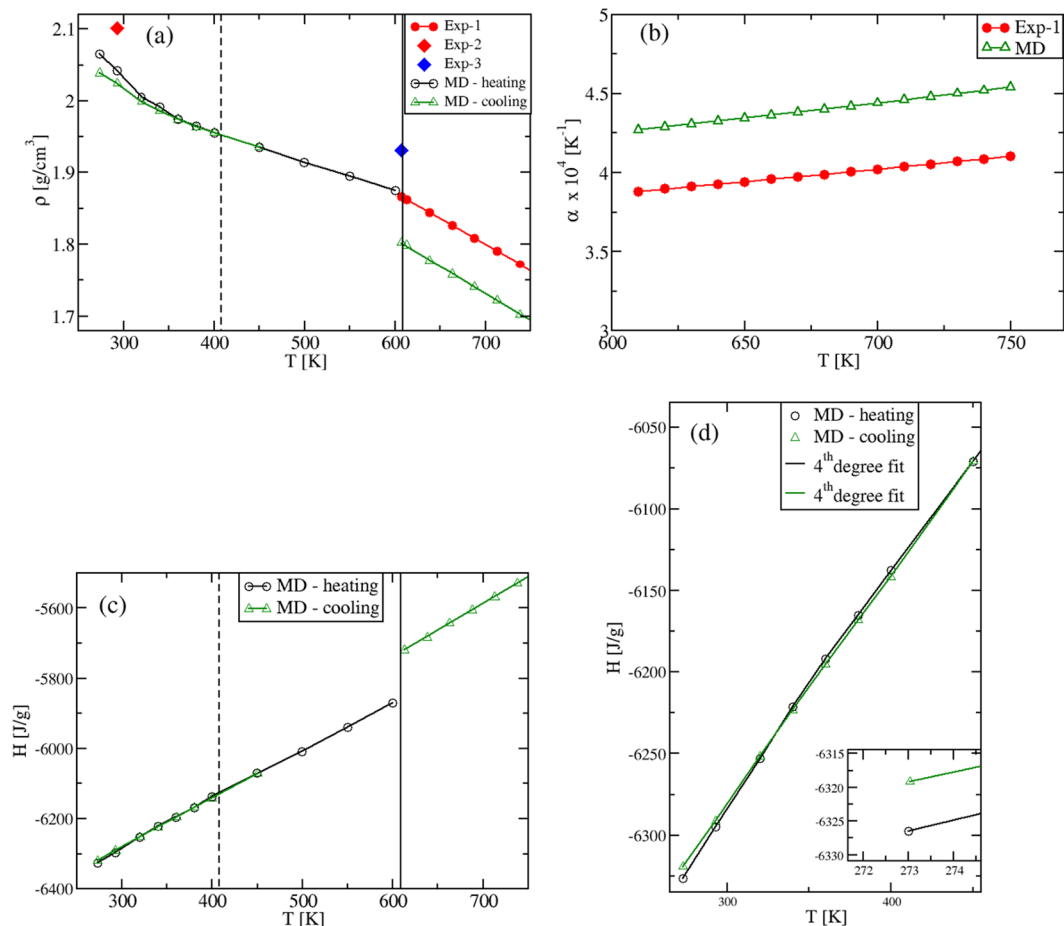


Figure 2. (a) Density $\rho(T)$, (b) thermal expansion coefficient $\alpha(T)$ and (c,d) enthalpy $H(T)$ of KNO_3 . $\rho(T)$ and $H(T)$ are calculated within $T = 273\text{--}750$ K at $P = 1$ atm; $\alpha(T)$ is computed in the liquid regime. (d) is a zoom of (c) within 273–450 K. Black and green plots are MD results calculated in this work. Red and blue full symbols are experimental results (Exp-1: ref.³⁶; Exp-2: ref.⁴⁹; Exp-3: ref.²⁷). Vertical dashed lines correspond to the α - KNO_3 to β - KNO_3 transition (at the experimental $T_{S-S}^{\text{exp}} = 403$ K), while full vertical lines indicate the melting transition (at $T_M^{\text{exp}} = 607$ K). In (a), the splitting of the two green and black plots in the region $T \approx [273, 345]$ K is due to the KNO_3 polymorphism, where two phases are obtained depending on the kinetic path followed by the system. In (c), we show the overall enthalpy behavior in all investigated phases. The two different sets of data (black and green symbols) are obtained to heating up and cooling down the system. Both are best fitted with 4th degree polynomials in the solid range, while in the liquid region we find a perfectly linear behavior. The inset in (d) shows that a lower enthalpy is associated to α - KNO_3 , which is more stable than γ - KNO_3 at $T = 273$ K.

Mass density and thermal expansion coefficient. Experimentally, solid KNO_3 shows three polymorphic forms at $P = 1$ atm²⁶: a stable form at 299 K, denoted α - KNO_3 ; a stable phase generated by heating at $T = 403$ K, β - KNO_3 ; and a third, different metastable phase γ - KNO_3 obtained by cooling down the system from high temperature, resulting from an alternative kinetic path.

As we aim to characterize the specific heats in various phases, we preliminary analyze the density $\rho(T)$ and the enthalpy $H(T)$ temperature behavior. The results are presented in Fig. 2. Focusing first on the solid phases between 273 K and ≈ 600 K, we find that by heating up the α - KNO_3 phase from $T = 273$ K, the calculated density shows a strongly non-linear behavior in the range $T = [273, 400]$ K, Fig. 2(a). This indicates the formation of a new phase, corresponding to β - KNO_3 . By cooling down the latter from $T = 450$ K, the density is once again non-linear, but the γ - KNO_3 phase is obtained at room temperature.

In the liquid region, the density $\rho(T)$ is, instead, a linear function with a MD slope that coincides with the experimental one²⁷. In this regime, our values confirm quantitatively the ones reported previously¹³. The slope, normalized by $\rho(T)$, gives the thermal expansion coefficient $\alpha(T)$, shown in Fig. 2(b). The difference between experiment and theory in $\alpha(T)$ reflects only the difference in the corresponding values of the density, which is within 5% in the entire T -range investigated (at $T = 293$ K, $\rho = 2.023$ g cm^{-3} , while $\rho^{\text{exp}} = 2.101$ g cm^{-3} ; at $T \approx 600$ K, $\rho = 1.87$ g cm^{-3} , while $\rho^{\text{ex}} = 1.867$ g cm^{-3}). A good agreement is also obtained for the volume change at the experimental melting point, $T_M = 607$ K. At $T_M^{\text{MD}} = 592.5$ K, the MD value is $\Delta V_m^{\text{MD}}/V_S^{\text{MD}} = 4.03\%$, while the experimental change is $\Delta V_m^{\text{exp}}/V_S^{\text{exp}} = 3.3\%$ ²⁷. Again, these density results confirm the ability of the inter-atomic potentials¹³ in describing the experimental findings.

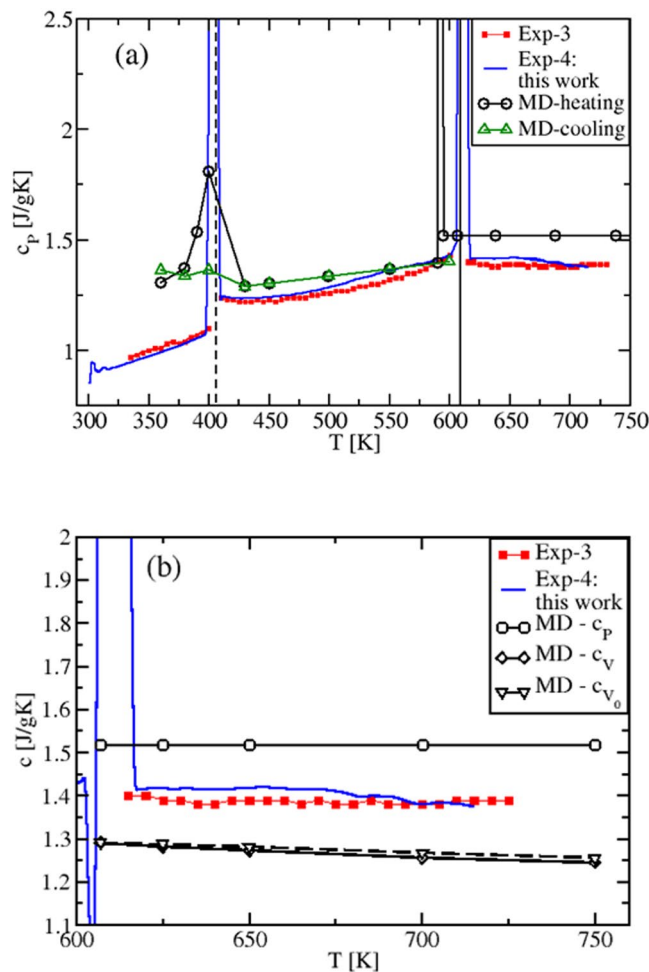


Figure 3. (a) Isobaric specific heat of KNO_3 , in the whole solid (at $P = 1$ atm) and liquid regimes investigated. In the solid phase, c_p is calculated both when heating (black) and cooling (green) the system. A transition peak is shown in correspondence of the solid-to-solid $\alpha\text{-KNO}_3 \rightarrow \beta\text{-KNO}_3$ phase transition ($T \approx 400$ K)²⁶ when heating, in excellent agreement with the experiments. (b) Specific heats c_p , c_v and c_{V_0} of KNO_3 in the liquid T -range only. The simulated c_p is found to be constant, while c_v and c_{V_0} are both decreasing with temperature. Exp-3: ref.⁴; Exp-4: this work.

Enthalpy. We next calculate the enthalpy $H(T)$ in the whole temperature interval. In Fig. 2(c,d), a non-linear T -behavior corresponding to the density one is found in the solid range. The two MD plots in Fig. 2(c) are obtained by heating up or cooling down the system, respectively (black and green symbols). The values at $T = 273$ K show that the stable phase is the $\alpha\text{-KNO}_3$ (Fig. 2(d) inset), while the metastable $\gamma\text{-KNO}_3$ phase should transform into the former with time²⁸. In the liquid phase we find the important result that our $H(T)$ data are perfectly linear with the temperature. Finally, by extrapolating the solid and liquid $H(T)$ to T_M , the computed value for the melting enthalpy is $\Delta H_M^{MD} = 130$ J/g, which is to be compared with the experimental value of $\Delta H_M^{\text{Exp}} \approx 100$ J/g⁴.

Specific Heats. By performing the derivative of the MD enthalpy plots (fitting polynomials for $H(T)$ were used), we now show the obtained specific heats (Fig. 3), and compare them with our experimental results and existing experiments⁴. The isobaric $c_p(T)$ is presented in Fig. 3(a). Remarkably, due to the $H(T)$ non-linearity in the solid regime, the calculated c_p shows a transition peak in correspondence of the solid-to-solid $\alpha\text{-KNO}_3 \rightarrow \beta\text{-KNO}_3$ transition ($T \approx 400$ K)²⁶ and, still in accordance with the experimental data, a slightly increasing behavior until the melting T_M is reached. Importantly, Fig. 3(b) shows that in the whole temperature range of liquid stability c_p has a constant value, $c_p^{MD} = 1.518$ Jg⁻¹ K⁻¹, in disagreement with previous theoretical results¹³.

Figure 3(b) also shows the MD predicted $c_v(T)$ and $c_{V_0}(T)$ behaviors calculated, respectively, at constant (V) and at fixed volume (V_0). The latter is chosen to be the volume immediately after the melting temperature²⁹. As it is clear from the internal energy of the liquid state (Eq. (5), Sec. 1.2), the $c_{V_0}(T)$ decrease is purely due to the smoothing and broadening of the peaks in the pair distribution functions $g_{ij}(r)$, while in the $c_v(T)$ decrease there is the additional contribution from the variation of $V(T, P = 1$ atm), via the density $\rho(T)$.

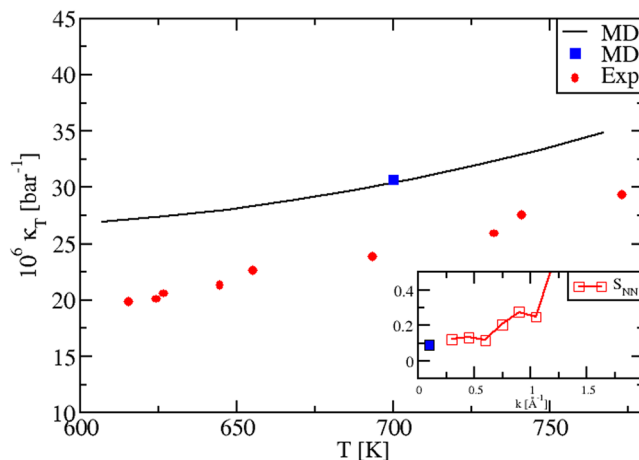


Figure 4. Isothermal compressibility $\kappa_T(T)$ of KNO_3 , calculated with *three* different methodologies. Exp: ref.⁵⁰. The black plot is calculated from the relation $\kappa_T = \alpha^2 T / [\rho(c_p - c_v)]$. The blue dot at $T = 700$ K is computed via an independent procedure and using $\kappa_T = -V^{-1}(\partial\langle V \rangle / \partial P)_T$. The blue dot is on top of the first plot, highlighting our internal consistency. In the inset, we report the $S_{NN}(k)$ Bhatia-Thornton structure factors^{25,32,33} calculated at $T = 700$ K. The blue dot corresponds to the previous one. We see that $S_{NN}(k)$ tends to the right limit for small wave vectors k , approaching a κ_T (blue dot) coming from a completely different calculation, confirming the validity of our numerical procedures.

In the gas-like approach to liquids^{24,25}, the $g_{ij}(r)$ smoothing and broadening correspond to less defined coordination shells around given ions, from which they can more easily escape or jump at increased temperature. In the solid-state approach of refs^{20–23}, they correspond to a shorter time between two consecutive ion jumps, known as the Frenkel time τ_F (and to a larger frequency ω_F). This results in a temperature decrease of the number of transverse oscillating modes, which has been identified as the main cause of the decrease of $c_{V_0}(T)$ ^{20–23}.

Since $c_p(T)$ can be written as $c_p(T) = c_v(T)(1 + \gamma\alpha T)$, where γ is the Grüneisen parameter and α is the coefficient of thermal expansion and since, typically, γ is almost T -independent³⁰, it follows that $c_p(T)$ is the product of a temperature decreasing term, $c_v(T)$, and a temperature increasing term containing αT ^{2,20}. As a result, $c_p(T)$ must be *less*, or *not at all* sensitive to temperature changes, as we actually find. This behavior is also consistent with the experimental results found for molten alkali and alkali earth halides³¹ that, as KNO_3 , belong to the class of low viscosity ionic liquids. Previous $c_p(T)$ values¹³ differ from our results, since $c_p(T)$ was determined by considering, on the top of the MD interaction model, internal degrees of freedom contributions to the kinetic ideal term that are T -dependent¹³.

The overall agreement between experimental data and MD results in $T = [400, 725]$ K is very good if compared to the accuracy found in the literature¹³, the difference being $< 8\%$. However, we note that the c_p experimental data are in between the c_p and c_v theoretical results and show a slight tendency to decrease and oscillate with increasing T . This could be a consequence of experimental conditions closer to constant V than to constant P (sealed and small sample holder used in DSC experiments).

Isothermal compressibility. Our calculations reproduce correctly also the temperature dependence of the isothermal $\kappa_T(T)$ in the liquid phase, Fig. 4. We evaluated $\kappa_T(T)$ by using *three* different procedures, fully illustrated in Methods Section 1.3. The black plot stems from the relation $\kappa_T = \alpha^2 T / [\rho(c_p - c_v)]$. The blue dot at $T = 700$ K is instead calculated via an alternative sequence of steps and the use of the equation $\kappa_T = -V^{-1}(\partial\langle V \rangle / \partial P)_T$. Importantly, we can see that these data perfectly superpose. This represents a severe test to check our numerical precision and consistency, for *all* thermostatic quantities not directly obtainable as MD averages. We have a further confirmation of this consistency. After a suitable rescaling (MS, Eq. (9)) the blue dot value was reported in the inset of Fig. 4, together with the $S_{NN}(k)$ Bhatia-Thornton structure factors^{25,32,33}, which we also calculated at $T = 700$ K. As it is well known^{25,32,33}, we have the relation $\frac{1}{\rho_N k_B T} \lim_{k \rightarrow 0} S_{NN}(k) = \kappa_T$. In the inset, we see that, indeed, our $S_{NN}(k)$ curve tends to the right limit for small wave vectors k , approaching the rescaled κ_T that comes from a separate calculation. Also in this case the internal consistency is evident.

Sodium Nitrate NaNO_3 . We present now our results for NaNO_3 . To a large extent they exhibit similar features found in KNO_3 .

Melting temperature. The NaNO_3 melting temperature is calculated to be $T_M^{MD} = 594$ K, which is higher than the experimental value $T_M^{Exp} = 581$ K²⁶, but still in a reasonable agreement. ref.¹³ reports 591 ± 18 K.

Mass density and thermal expansion coefficient. The mass density results are shown in Fig. 5(a). Also in this case, the experimental data in the solid range have a strong non-linear behavior, as in KNO_3 . In fact, at $T = 433$ K a second-order phase transition begins from the low temperature stable phase, denoted II- NaNO_3 , to the high temperature phase, I- NaNO_3 ³⁴. The transition is complete at $T = 544$ K²⁶, and it is due to the activation of the

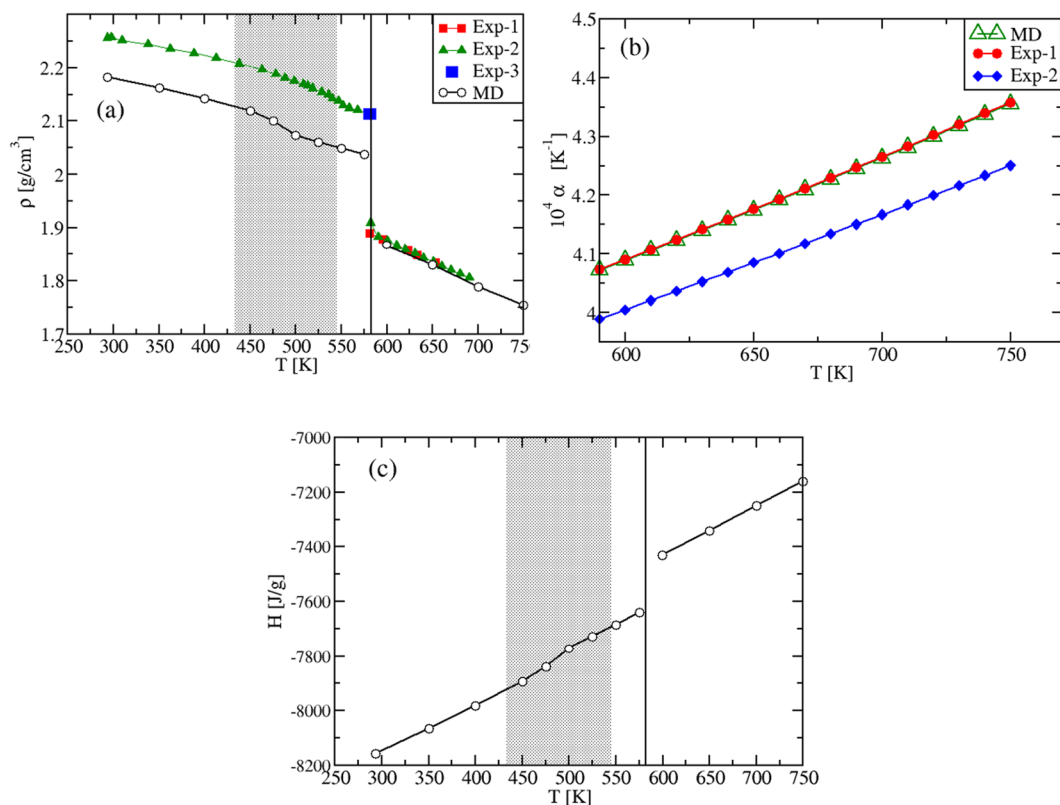


Figure 5. (a) Density $\rho(T)$, (b) thermal expansion coefficient $\alpha(T)$ and (c) enthalpy $H(T)$ of NaNO_3 . $\rho(T)$ and $H(T)$ are calculated in the full temperature range at $P = 1$ atm, $\alpha(T)$ in the liquid phase. Black and green plots with empty symbols are MD results calculated in this work. Full symbols are experimental results; Exp-1: ref.³⁶; Exp-2: refs.^{2,51}; Exp-3: ref.²⁷. In (a) and (c) vertical full lines indicate the experimental melting transition ($T_M^{\text{exp}} = 581$ K), while shaded regions correspond to the second-order $\text{II-NaNO}_3 \rightarrow \text{I-NaNO}_3$ phase transition (see text). The enthalpy MD results in the solid phase are fitted by a 4th degree polynomial, while those in the liquid phase by a linear T -function. In (b), the MD data superpose with Exp-1, while the difference with Exp-2 is around 2%.

rotational degrees of freedom of the nitrate groups³⁵. In this temperature range, the theory-experiment discrepancy is found to be less than 4% at $T = 293$ K ($\rho^{\text{MD}} = 2.181$ g cm^{-3} , while $\rho^{\text{exp}} = 2.257$ g cm^{-3}), and the strong non-linearity is also well reproduced. Also in this case our values confirm quantitatively the ones reported previously¹³. In the liquid phase, both the $\rho(T)$ linear behavior and the set of experimental data are perfectly reproduced. However, we need to consider that in the liquid range, the experimental data refer to systems where, intrinsically, both sodium nitrates and nitrites are present (see ref.² and references therein), while our MD results refer to pure NaNO_3 . Still, although this level of precision might be quite accidental, the interaction potentials used show to be, once more, highly accurate. This is also true for the liquid branch of the thermal expansion coefficient, shown in Fig. 5(b), where we see that the theoretical and experimental³⁶ results essentially superpose.

Enthalpy. The enthalpy $H(T)$ is reported in Fig. 5(c). As for the density, the enthalpy is non-linear in the solid phase and linear in the liquid region. By extrapolating the solid and liquid enthalpies to the experimental $T_M^{\text{exp}} = 581$ K, a value of $\Delta H_M^{\text{MD}} = 173$ J/g is obtained, in quantitative agreement with the experimental value, $\Delta H_M^{\text{exp}} \in 172 - 187$ J/g².

Specific Heats. The c_p values are shown in Fig. 6. In the solid phase, c_p increases with T , and shows a peak in the same region where the second-order phase transition is experimentally observed^{26,34}. This transition is also evident from the $c_p(T)$ increase observed in our DSC experimental data, also reported in the same Figure. In the liquid phase, $c_p(T)$, analogously to KNO_3 , has a constant value for all the investigated temperatures ($c_p^{\text{MD}} = 1.805$ J g^{-1} K^{-1}), as shown in Fig. 6(a,b). Experimental $c_p(T)$ data are either constant, as the MD results, or exhibit a decreasing behavior. The comparison between our experimental and theoretical results show a difference of $\approx 7\%$. Instead, our MD $c_v(T)$ and $c_{V_0}(T)$ show a decreasing behavior.

Isothermal compressibility. Finally, as shown in Fig. 7, the T -behavior of the experimental isothermal compressibility $\kappa_T(T)$ in the liquid regime is also well reproduced by our MD modeling. A similar self-consistency test as for KNO_3 , based on the use of three calculation procedures was performed for NaNO_3 . The test was successful,

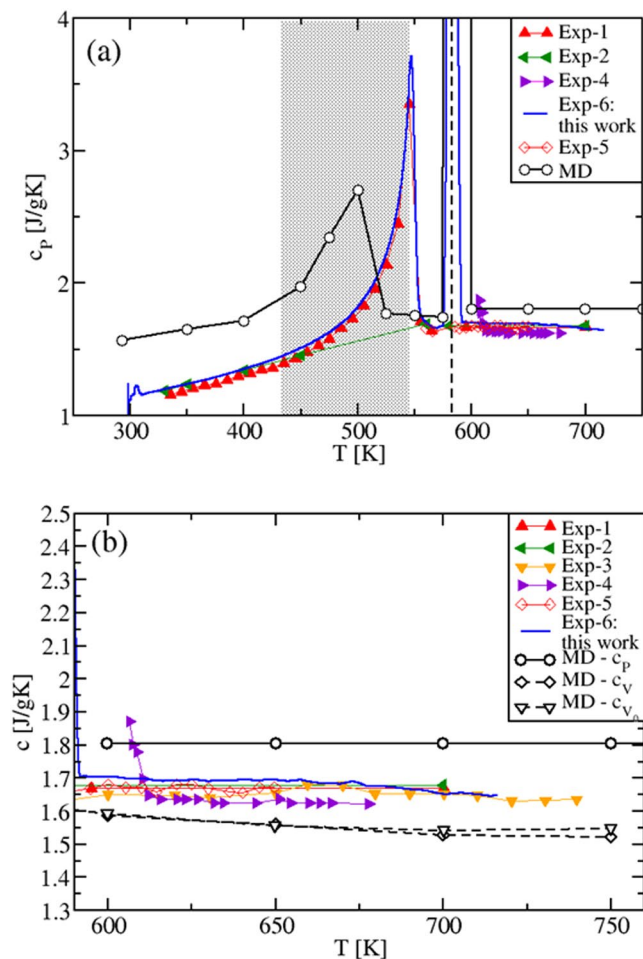


Figure 6. (a) Specific heat of NaNO_3 in the whole solid (at $P = 1$ atm) and liquid regime investigated. In the solid phase, c_p increases with T and shows a peak in the same region where the second-order phase transition II- NaNO_3 to I- NaNO_3 is experimentally observed. The dashed vertical line corresponds to the experimental melting transition. (b) Specific heats c_p and c_v of NaNO_3 in the liquid T -range only. As in KNO_3 , the simulated c_p is found to be constant, while c_v and c_{v_0} are decreasing with temperature. Exp-1: ref.⁴; Exp-2: ref.⁷; Exp-3: ref.⁶; Exp-4: ref.⁵²; Exp-5: ref.⁵³.

as shown by the coincidence of the black plot and the blue dot in Fig. 7 and by the correct behavior of the Bhatia-Thornton structure factors $S_{NN}(k)$, tending to κ_T at the $k \rightarrow 0$ limit. Hence, all the considerations on accuracy and precision made for the KNO_3 isothermal compressibility apply here too.

Eutectic and “Solar” Mixtures. Molten salt mixtures are technologically extremely relevant, especially when considered in their liquid phase. The characterization of their thermostatic properties is important not only for a fundamental understanding of the physics of ionic liquids at high temperature, but also for energy applications in any system containing a heat storage component. In this respect, it is also important the development of viable simulation methods to determine technological relevant binary and ternary molten salt eutectics³⁷. In the following we will calculate, in the liquid phase only, the thermostatic properties of two relevant nitrate molten salt mixed systems: the *eutectic* and the “*solar*” mixture. Emphasis is given on the specific heats thermal behavior, where the available experiments still exhibit a high degree of controversy⁴⁻⁷.

The eutectic NaNO_3 - KNO_3 mixture has the chemical composition $\text{Na}_{0.5}\text{K}_{0.5}\text{NO}_3$. Due to the lower mass of Na, this corresponds to a 45.67% NaNO_3 -54.33% KNO_3 weight percentage composition. The “solar salt” mixture has a higher content of Na, with a chemical composition of $\text{Na}_{0.641}\text{K}_{0.359}\text{NO}_3$ and a weight percentage of 60% NaNO_3 -40% KNO_3 .

Mass densities. The density plots for both systems are shown in Fig. 8. The theory-experiment agreement is satisfactory. However, while for the pure salts the difference between experimental and modeling results is the same in the whole liquid phase, here the discrepancy increases as the temperature increases. This behavior could be related to the use of the Lorentz--Berthelot approximation³⁸ to describe the crossed interaction between Na^+ and K^+ particles, which is the only approximation introduced in passing from the pure components to the mixtures.

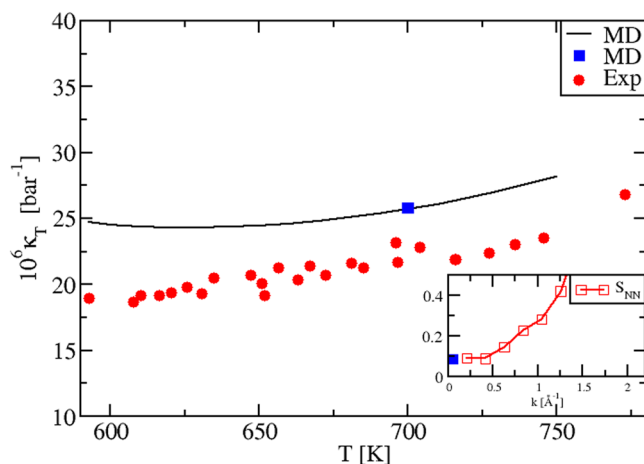


Figure 7. (a) Isothermal compressibility $\kappa_T(T)$ of NaNO_3 , calculated with three different methodologies, as in KNO_3 (see Fig. 4 caption). Exp: ref.⁵⁰. The black plot is calculated from the relation $\kappa_T = \alpha^2 T / [\rho(c_p - c_v)]$. The blue dot at $T = 700$ K is computed via an independent procedure and using $\kappa_T = -V^{-1}(\partial \langle V \rangle / \partial P)_T$. As in KNO_3 , the blue dot is on top of the first plot and the Bhatia-Thornton structure factors shown in the inset tend to κ_T in the $k \rightarrow 0$ limit.

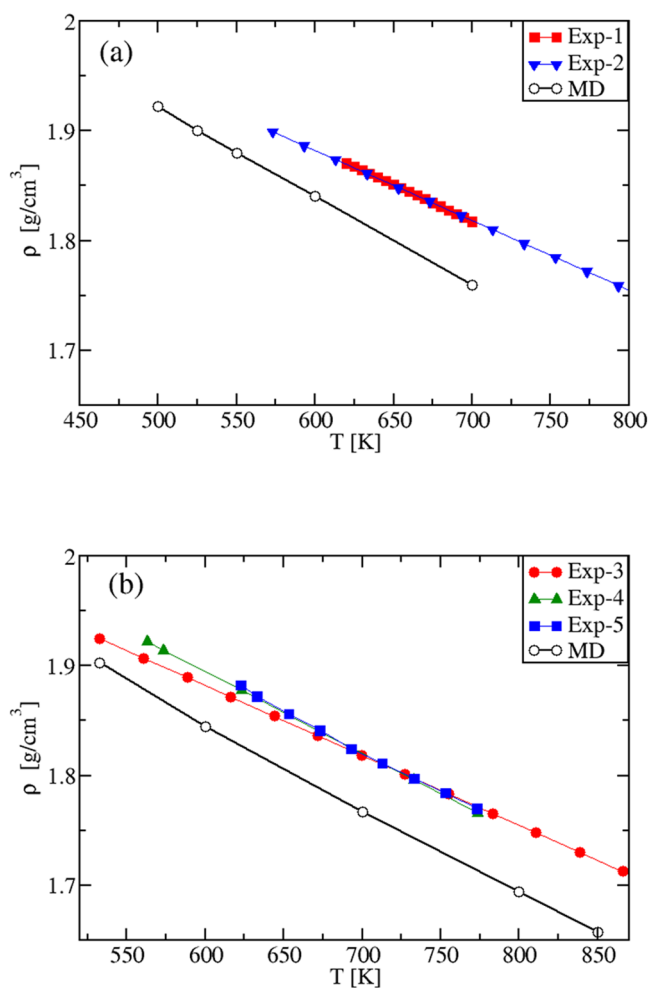


Figure 8. (a) Density $\rho(T)$ of (a) the eutectic mixture and (b) the “solar” mixture in the liquid phase; Exp-1: ref.⁵⁴; Exp-2: ref.⁵⁵; Exp-3: ref.⁹; Exp-4: ref.⁵⁶; Exp-5: ref.⁵⁷.

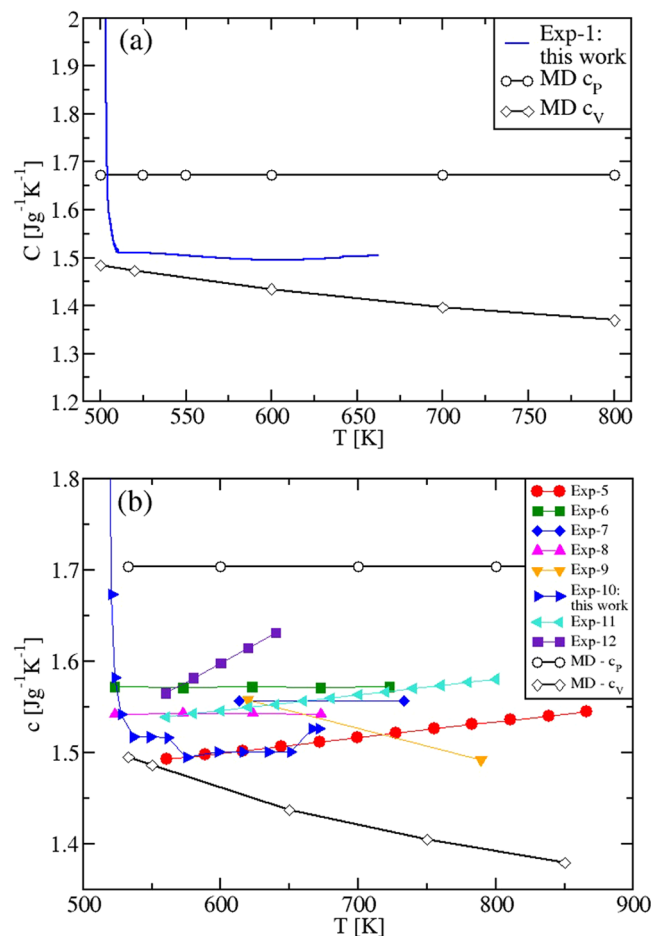


Figure 9. (a) Specific heats c_p and c_v of the eutectic mixture in the liquid phase; Exp-1: this work. (b) Same as (a) but for the “solar” mixture. In this latter case, the experimental picture is rather complex, with decreasing/constant/increasing/oscillating behaviors of the specific heat with the temperature. Our calculated value for c_p and c_v are constant and decreasing, respectively. This is similar to what found in the pure salts. Note, in particular, that our calculations revisit empirical relations used industrially⁹, showing an increasing c_p (turquoise left triangles). Exp-5: ref.⁶; Exp-6: ref.⁷; Exp-7: ref.⁴; Exp-8: ref.⁵; Exp-9: ref.⁶; Exp-10: this work.; Exp-11: ref.⁹; Exp-12: ref.¹⁹.

Specific heats. The specific heats of the mixtures are shown in Fig. 9(a,b). Importantly, we found again that the calculated values of c_p are *temperature independent*. They are $1.673 \text{ J g}^{-1} \text{ K}^{-1}$ and $1.704 \text{ J g}^{-1} \text{ K}^{-1}$ for the eutectic and the “solar” mixture, respectively. The specific heat $c_v(T)$, instead, is predicted to be a decreasing function of T . As the simulations allow to compute the specific heats by keeping either the volume or the pressure strictly constant, we speculate that all the observed systematic discrepancy between the $c_p(T)$ experimental and MD results can be due to the fact that in DSC experiments aimed at measuring $c_p(T)$, the control of the experimental conditions is rather challenging, especially in the case of ionic liquids. For instance, inside the sealed sample holders partially filled by a small amount of sample, a very high and variable pressure can be generated, with the sample changing its volume as the temperature is changed. Ionic samples present extra difficulties due to the non-wetting of the sample holder surfaces. This complexity is reflected in the variety of $c_p(T)$ behaviors with temperature, as measured by DSC. As shown in Figs 3(b), 6(b) and 9(a,b), $c_p(T)$ is found to decrease, to be constant and to increase. Our MD results clarify, once for all, that working at constant pressure a *constant value* of $c_p(T)$ is produced, while at constant volume a decreasing $c_v(T)$ is predicted.

As a conclusion for technological applications, we then propose to reconsider the use of empirical equations showing a $c_p(T)$ temperature-dependent behavior for any molten K-Na nitrate mixture (see, e.g., the *increasing* $c_p(T)$ used industrially, Exp. 11⁹ in Fig. 9(b)). We estimate that such a behavior, bringing, e.g., to a 5% overestimate of the real $c_p(T)$ value, corresponds to a loss of 0.75 h/day of electricity production in a CSP plant with a “solar” salt tank able to store energy for 15h. On a yearly basis (and for a typical 50 MW plant), this translates in the considerable loss of ≈ 12 GWh/year in the electricity production.

Due to the fact that the calculated c_p values of the pure and mixed salts are T -independent, c_p can be plotted against the weight fraction x of KNO_3 present in the mixture. This is done in Fig. 10, where we see that by interpolating the calculated values of the four investigated compositions (pure NaNO_3 , eutectic, “solar salt” and pure KNO_3), c_p changes linearly. Although the experimental data in Fig. 10 refer to different temperatures, a linear

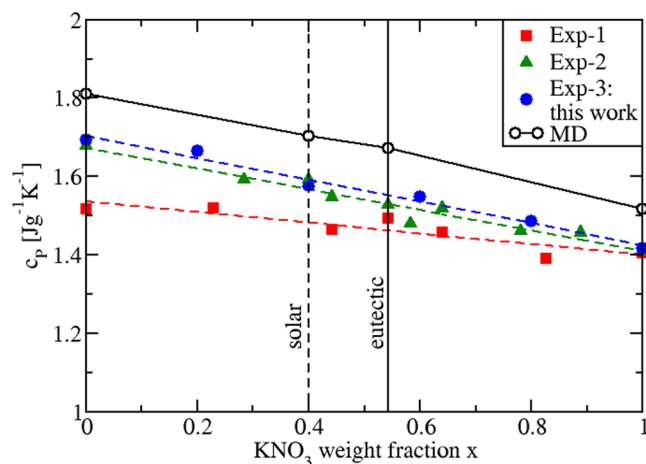


Figure 10. Specific heat $c_p(x)$ of as a function of the KNO_3 weight fraction x (black plot). The vertical dashed line corresponds to the “solar” mixture, the plain to the eutectic. Dashed plots are linear interpolations of the experimental results; Exp-1: ref.⁵⁸; Exp-2: ref.⁷; Exp-3: this work. Due to their T -dependence, all experimental values refer to averaged T values.

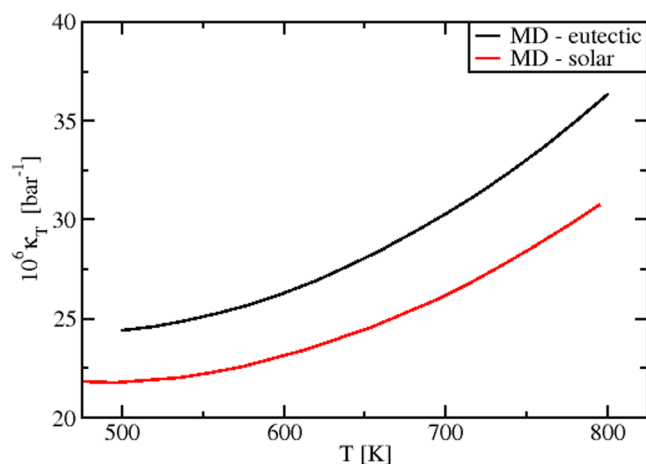


Figure 11. MD predicted isothermal compressibility, $\kappa_T(T)$, for the eutectic and “solar” mixtures.

behavior can be also identified. We then conclude that mixtures of KNO_3 and NaNO_3 behave as ideal mixtures. Thus, to determine the $c_p(x)$ of any mixture, no extra measurements or simulations are needed, as it is sufficient to consider a linear combination of the pure salts values with their respective weight fractions, i.e. $c_p(x) = xc_p^{\text{KNO}_3} + (1-x)c_p^{\text{NaNO}_3}$.

Isothermal compressibility. The MD values of the isothermal compressibility $\kappa_T(T)$ are reported in Fig. 11. These data are the first prediction appearing in literature. By considering the accuracy of the MD results for the pure salts, highlighted in previous sections, they can be used as reference for further studies, both experimental and theoretical.

Discussion

In this work, by combining classical molecular dynamics (MD) simulations and differential scanning calorimetry (DSC) experiments, we investigated the thermodynamic properties of nitrate molten salts, technologically relevant materials for thermal energy storage applications. We focussed, in particular, on the thermal behavior of the specific heats of KNO_3 , NaNO_3 and their eutectic and “solar” mixture, the latter known as “solar salt”. The motivation of our work is twofold: First, to the best of our knowledge, theoretical calculations about the thermodynamic properties in the solid and liquid phase of these materials are largely missing. Second, there is a general lack of consensus about the experimentally measured specific heats as a function of temperature, especially for what concerns c_p in the liquid phases.

To address these issues, we first computed the mass density, the enthalpy and the thermal expansion coefficient of pure nitrate salts, as a function of temperature. Moreover, we calculated the melting transition temperature T_M

and the enthalpy and the volume changes at T_M . We obtained an accurate theoretical description, reproducing quantitatively the available experimental data. This allowed to reproduce several non-trivial features of solid-solid and solid-liquid phase transitions in the case of the pure salts.

Next, we characterized the specific heats in the pure salts, and, due to their technological relevance, in the mixtures. For all investigated liquid systems, we found a *constant* value of $c_p(T)$, while $c_v(T)$ is weakly decreasing with temperature.

Finally, we calculated the isothermal compressibility $\kappa_T(T)$, encompassing other thermostatic properties, in excellent agreement with the experiment. This fact, together with a careful, self-consistency check based on *three* independent procedures to calculate this quantity, fully validates our MD numerical scheme. Thus, we expect that our results for the eutectic and “solar” mixtures have the same degree of accuracy.

The constant value of $c_p(T)$ in the liquid regime clarifies a complex experimental picture, especially in the case of the “solar” mixture, where more experimental data are available. In view of this, for this material we suggest to reconsider the empirical T -increasing function $c_p(T) = \gamma + \delta T$, used in the design of thermal energy storage components.

For the eutectic and “solar” salt our results also allow to say that these materials behave as ideal mixtures, i.e. the c_p of *any* mixture can be obtained from the c_p of the pure salts only.

We believe that our results are of general validity and not limited to the class of nitrate molten salts. They confirm many temperature trends observed in the thermostatic properties of strongly interacting liquids (e.g. the condensed phases of alkali halides³¹). They provide guidelines for researchers who perform experiments on the development of salt-based fluids for thermal energy storage. These include bulk nanomaterials and colloidal suspensions in ionic compounds.

Future studies will require theoretical reference data and validated models about basic materials that compose more complex nanomaterials, as the ones provided in this work.

Methods

Computational Methods. The used classical MD model is based on a version of the Fumi and Tosi pair interaction potential^{39,40}, i.e. the Buckingham potential, superimposed to a Coulomb potential. The inter-atomic parameters of the Buckingham potentials are taken from S. Jayaraman *et al.*¹³. This parametrization has been chosen because: (i) it reproduces the liquid and crystal phase densities of the pure KNO_3 and NaNO_3 within 4% of the experimental data¹³; (ii) it reproduces the MD partial pair distribution functions, $g_{ij}(r)$, of the pure NaNO_3 evaluated by A.K. Adya *et al.*⁴¹ with a Born-Mayer-Huggins type of interaction potential. The latter reproduces the experimental structure factor extracted from the measured X-ray diffraction intensity⁴¹. No further refinements of the interaction parameters, and no other approximations beyond the Lorentz–Berthelot approximation³⁸, needed for the cross interaction parameters in the mixture case, are made. The model is sufficiently accurate for the purposes of the present study. Simulations have been performed with the LAMMPS code^{42,43}. Initial solid configurations are taken from ref.¹³. The NaNO_3 initial solid configuration at $T = 293$ K corresponds to the rhombohedral $R\bar{3}c$ group with $Z = 6$, $\mathbf{a} = 5.070 \text{ \AA}$, $\mathbf{c} = 16.82 \text{ \AA}$. The KNO_3 initial solid configuration at $T = 293$ K corresponds to the orthorhombic $\text{Cmc}2$ group with $Z = 16$, $\mathbf{a} = 10.825 \text{ \AA}$, $\mathbf{b} = 18.351 \text{ \AA}$, $\mathbf{c} = 6.435 \text{ \AA}$. The initial liquid configurations have been generated with the PACKMOL package⁴⁴. To study the pure salts, systems with 600 cations and 600 NO_3^- ions, for a total of 3000 particles, were constructed. To study the mixtures, 600 NO_3^- ions have been used while the cation numbers were 300 Na^+ and 300 K^+ for the equimolar mixture, and 384 Na^+ and 216 K^+ for the solar mixture. A time-step of 1 fs has been used. Systems were equilibrated using 10^6 time-steps and run with further $10^6 - 2 \times 10^6$ time-steps. For the solid (liquid) systems, equilibrated configurations at the lowest (highest) studied temperature were used as input for the closest next higher (lower) temperature. Other relevant parameters used are: Nosé-Hoover barostat time constant 0.5 ps; Nosé-Hoover thermostat time constant 0.1 ps; Buckingham and Coulomb interaction cutoff distance $r_c = 12 \text{ \AA}$ for systems with K^+ ions, and $r_c = 11 \text{ \AA}$ for other cases; long-range force calculation accuracy 10^{-4} . Production runs in NPT simulations were considered suitable for analysis only when the averaged equilibrated pressure was within $\langle P \rangle = 1 \pm 1 \text{ atm}$. Within this range, the change in the averaged $\langle H \rangle$ is $\leq 1 \times 10^{-2}\%$.

Thermodynamic Properties. Thermodynamically, the specific heats c_v and c_p are defined as:

$$c_v = \frac{1}{N} \left(\frac{\partial E}{\partial T} \right)_{V,N}, \quad (1)$$

$$c_p = \frac{1}{N} \left(\frac{\partial H}{\partial T} \right)_{P,N}, \quad (2)$$

where E is the internal energy, H the enthalpy and N the mole number, which is kept constant. These quantities are linked by the relation:

$$c_p = c_v + \frac{1}{\rho} \frac{\alpha^2}{\kappa_T} T, \quad (3)$$

where $\alpha = V^{-1}(\partial V/\partial T)_P$ is the coefficient of thermal expansion, $\rho = N/V$ is the density and $\kappa_T = -V^{-1}(\partial V/\partial P)_T$ the isothermal compressibility. Eq. (3) can be also written in the form:

$$c_p = c_v(1 + \gamma\alpha T), \quad (4)$$

were the Grüneisen parameter, $\gamma = \alpha/(\rho\kappa_T c_v)$, is introduced. Typically, $\gamma \approx 1$ and it is almost T -independent³⁰.

In the NVT ensemble, the internal energy E in Eq. (1) is expressed by the relation:

$$E = E_{Kin}(T) + E_{Pot}(T) = E_{Kin}(T) + 2\pi\rho TN \sum_{i,j} x_i x_j \int E_{ij}^{pot}(r) g_{ij}(T, r) r^2 dr, \quad (5)$$

where x indicates the number fraction and $g_{ij}(T, r)$ the ij pair distribution function. If in the considered T -range all the kinetic degrees of freedom are activated, E_{Kin} is a linear function of T giving a constant term contribution to $c_v(T)$. Then the temperature contribution to $c_v(T)$ only arises from the T -dependence of the density ρ and of the pair distribution functions $g_{ij}(r)$ appearing in the E_{Pot} term. To separate the temperature effects of these two quantities, two sets of simulations have been conducted. In the first set, a liquid density ρ_0 , chosen at a density close to the freezing point, is kept fixed for all the investigated T ; in the second set, the $\rho(T)$ values obtained from the NPT equilibration run are used.

Simulation Methods and Self-Consistent Check. To calculate the specific heats and other thermodynamic properties in the liquid phase, the simulation is performed by a step-by-step cooling procedure. First, we worked in the NPT ensemble. Starting from a random distribution of particles⁴⁴, the system is equilibrated at the highest temperature, usually the experimental decomposition temperature where the salt molecules break. The temperature is then decreased, and the equilibrated configuration of the previous T -step is used as a starting configuration for the next T . All equilibrated configurations are used to perform production runs and data analysis. When necessary, these NPT configurations are used as input for NVT ensemble simulations.

As for the specific heats, there are several ways to determine them from ensemble averages of MD trajectories³⁸. In this work, the direct evaluation via the relations

$$c_V = \left(\frac{\partial \langle E \rangle_{NVT}}{\partial T} \right)_{N,V}, \quad c_P = \left(\frac{\partial \langle H \rangle_{NPT}}{\partial T} \right)_{N,P}, \quad (6)$$

is preferred due to its stability and reliability. Their evaluation is functional to a scheme aimed at the determination of all thermodynamic properties. Moreover, a final self-consistency check is performed.

In detail:

1. Fix the pressure, $P = 1$ atm, and the number of moles N .
2. Perform NPT simulations for a set of temperatures T .
3. Extract the functions: $V(T)$, $\rho(T)$, $\alpha(T) = V^{-1}(\partial \langle V \rangle / \partial T)_P$, $H(T)$ and $c_p(T)$ from Eq. (6).
4. For each value $V(T_i)$ perform four NVT simulations at temperatures $T_i \pm \Delta T$ and $T_i \pm 2\Delta T$.
5. Extract $c_v(T_i)$ from Eq. (6), via a four-point differentiation relation of the total energy $E(T)$ ⁴⁵.
6. Repeat the previous point for a set of temperatures and obtain the function $c_v(T)$.
7. Calculate the isothermal compressibility κ_T , via *three* different procedures. *First*, for each T_i perform a set of NPT simulations in the pressure interval $P \in [1, 600]$ atm. Use the equation

$$\kappa_T = -V^{-1}(\partial \langle V \rangle / \partial P)_{T_i}, \quad (7)$$

to extract $\kappa_T(T_i)$ from a linear differentiation.

8. Repeat the previous point for a set of temperatures and obtain the function $\kappa_T(T)$.
9. Self-consistency check:

- (a) Compare the $\kappa_T(T)$ values from step 8 with a *second* set of values, from the equation

$$\kappa_T = \alpha^2 T / [\rho(c_p - c_v)] \quad (8)$$

where $\alpha(T)$, $\rho(T)$ and $c_p(T)$ are obtained from step 3, and $c_v(T)$ from step 6.

- (b) Evaluate the percentage difference of κ_T calculated in the two ways. This difference is a severe test for: (i) the achievement of equilibrated MD configurations (slope of the equilibrated energy functions $\langle 10^{-8} \div 10^{-9}$); (ii) the numerical precision of the procedures to determine c_p , c_v , α , and κ_T itself.
- (c) κ_T can also be determined via a *third* procedure, from the total number density Bhatia-Thornton structure factor, $S_{NN}(k)$ ^{25,32,33}.

$$\kappa_T = \frac{1}{\rho_N k_B T} \lim_{k \rightarrow 0} S_{NN}(k), \quad (9)$$

where

$$S_{NN}(k) = 1 + \rho [x_c^2 \tilde{h}_{cc}(k) + x_a^2 \tilde{h}_{aa}(k) + 2x_c x_a \tilde{h}_{ca}(k)], \quad (10)$$

In these equations, ρ_N is the number density and $\tilde{h}_{\alpha\beta}(k)$ are Fourier transform of the cation and anion pair correlation functions $h_{\alpha\beta}(r) = g_{\alpha\beta}(r) - 1$. Here, the pair distribution functions $g_{\alpha\beta}(r)$ are obtained from the NVT

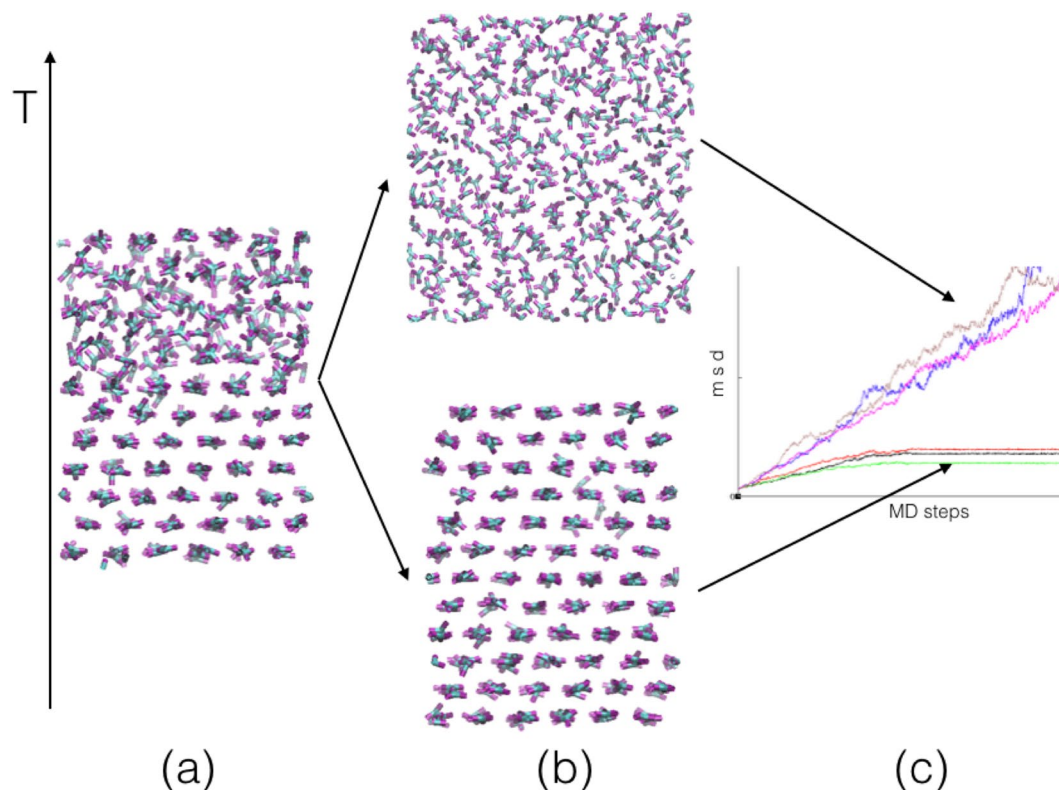


Figure 12. Procedure to calculate the solid-to-liquid transition temperature T_M by simulating the temporal evolution of a two-phase system. (a) System where the two phases coexist. (b) Depending whether the simulation temperature is $T_S > T_M$ or $T_L > T_M$, the system will evolve, respectively, either towards a solid phase (lower configuration) or a liquid phase (upper configuration). (c) Mean squared displacement (*msd*) as a function of the MD time steps: a zero, constant or changing slope indicates, respectively, a solid phase, a liquid phase and an evolving phase towards one of them.

averages $x_\alpha x_\beta \rho g_{\alpha\beta}(r) = N^{-1} \left\langle \sum_{i_\alpha} \sum_{j_\beta} \delta(r + r_{i_\alpha} - r_{j_\beta}) \right\rangle$. This calculation of κ_T through microscopic structural quantities, is a further check of the overall numerical scheme precision.

Calculations in the solid phase follow the same lines sketched for the liquid phase. The only difference is in the sequence of the MD runs, as in this case, in general, the simulations at constant pressure were performed as a step-by-step *heating* procedure. As for KNO_3 , we additionally adopted a step-by-step *cooling* procedure. In the initial configuration at the lowest temperature ($T = 300$ K), we considered the energetically stable crystallographic configuration at that temperature^{13,26}.

Method to Simulate the Melting Transition Temperature. To calculate the solid-to-liquid transition temperature T_M , we adopted an approach based on the direct simulation of a two-phases coexistence, with an explicit interface (Fig. 12). This approach has proven to be robust and reliable for systems of large size in particle number^{46–48}. Figure 12(a) shows a system with solid and liquid phases, previously (and separately) equilibrated at a temperature close to the expected T_M . By performing a simulation at $T_L > T_M$, the interface will move in order to suppress the solid phase (Fig. 12(b), upper panel), while at $T_S < T_M$, the interface will move in order to suppress the liquid phase (Fig. 12(b), lower panel). The evolution of the two-phase system towards either the liquid or the solid phase is shown in Fig. 12(c). Here the mean squared displacement (*msd*) of the atoms is plotted as a function of the MD time steps. The solid will be characterized by a zero slope and the liquid by a slope related to the liquid self-diffusion constant. The change in slope for increasing time steps will characterize the two-to-one phase transition, in both cases. After having chosen a suitable temperature interval (which must include T_M), the procedure to obtain the transition temperature consists in starting from the configuration in Fig. 12(a) and performing a set of simulations by slowly decreasing (increasing) T_L (T_S) until the difference $\Delta T = T_L - T_S$ is small enough. In our simulations we chose $\Delta T \approx 5$ K, as smaller values make our results unstable and strongly dependent on the coupling rates with the thermostat and the barostat. This small value defines the accuracy of the calculated melting temperature, $T_M = (T_L + T_S)/2$. This approach will also allow to calculate the volume and enthalpy changes at the transition, respectively $\Delta V_M = V_L(T_M + \Delta T/2) - V_S(T_M - \Delta T/2)$ and $\Delta H_M = H_L(T_M + \Delta T/2) - H_S(T_M - \Delta T/2)$.

Experimental. For the four investigated systems, we have performed a set of differential scanning calorimetry measurements (DSC). High purity sodium nitrate and potassium nitrate were provided by Sigma Aldrich and the salts were used without any further purification for the present study. In order to remove the final traces of moisture,

the samples were heated at 293 K with a heating plate located inside a globe box, and then the samples were encapsulated using hermetic Tzero aluminium lids and pans at argon atmosphere. Pure salt, standard sapphire and a reference (only the Al crucible) were hermetically sealed at argon atmosphere. The sapphire and the samples weights were measured by using a microbalance to 4 decimals in milligram (Mettles Toledo. X6TU Model). The specific heat values of all the samples were measured by using modulated differential scanning calorimeter (MDSC) (TA instruments, Q2000) with specific heating program. The encapsulated samples were heated at 723 K and kept isothermal for 10 minutes (to stabilize the heat flux signal). Before that, Tzero heat flow was implemented at this temperature and the sample was equilibrated at 298 K and then ± 1 K was executed every 120 seconds and stay again isothermal for 10 minutes. Finally, 2 K/min heat ramp was implemented till reach at 723 K.

Data availability. The datasets generated during and/or analyzed during the current study are available from the corresponding author on reasonable request.

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Author Contributions

B.D.A. conceived and performed the theoretical calculations, which have been extensively discussed with A.F. M.K. and N.G. conducted the experiments. B.D.A. and A.F. analyzed the results and wrote the manuscript.

Additional Information

Competing Interests: The authors declare no competing interests.

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